Chapter 8
Analyzing the Sample Path

The QSIM application provides some built-in analysis capabilities. You can obtain sample means, variance estimates, and other simple statistics on several measures of performance including time spent in system components and resource utilization. You can also display simple lineplots, histograms, and boxplots to dynamically observe system behavior.

An additional feature is the ability to accumulate the sample paths in SAS data sets. See Chapter 7, “Saving and Restoring,” for more information. With these data in data sets, you can write your own programs to do more sophisticated analyses.

When calculating statistics, QSIM uses the following measures of system performance:

- number in a queue
- time in a queue
- number of multiple-servers busy
- server utilization
- time in service
- time in the system.

In addition, statistics can be calculated on samples of random variables, which are user-defined attributes.

To illustrate some of the analysis features, this chapter uses the multiple-server, single-input queueing model shown in Figure 8.1.

![Figure 8.1. A Single Queue 3-Server Model](image)
The inter-arrival time distribution is $\mathcal{E}(0.33)$ and the service time distribution for each server is $\mathcal{E}(1)$. Transactions queue in a FIFO discipline and go to the first available server. This corresponds to the type of queueing that you encounter at check-in in many airports.

**Running a Simulation**

Suppose that you have built the model in Figure 8.1. You start and stop this simulation using the button on the command panel in the simulation window. The button starts the simulation by sending a start message to each of the components in the model. Similarly, the button stops the simulation.

![Figure 8.2. The Command Panel and Buttons](image)

Also note that the button stops and resets the simulation by sending the reset message to each component. But first it stops the simulation, resets the simulation clock, and removes all pending actions. For example, all queues are emptied and transactions in service are discarded.

The button toggles animation on and off. Animation is one effective way to validate a model. You simply turn animation on and observe the simulation behavior. In addition, you can add Triggers and StringHolder to display and print state information to help you with model validation.

Another way to control the simulation is with the Component Control Panel as shown in Figure 8.3.
Notice the buttons on the right side of the control panel. When any of these buttons are clicked a message is sent to each of the selected components. For example, you can select a component from the Components list box and start it only by clicking the Start button. It sends the start message to the selected component. This is typically not the way to start the simulation since not all components will be started, but it is the typical way to analyze component performance with the Analyze button.

Statistics on Component State

The queues and servers are two component types for which performance measures are typically of interest. For queues you want to know the distribution on queue length, and for servers you want to know about server utilization. Other performance measures that may be of interest are time in the queue and time in service. These are discussed in the “Statistics on Transaction State” on page 81.

There are two ways you can obtain statistics on queue length and server utilization. One way uses the chart components and the other uses the Simulation control panel shown in Figure 8.3. When the data collection status is “On” in this control panel, all changes of state are recorded to a SAS data set. These data can be summarized through the Simulation Control Panel and through the Analyze button.

Queue Length

The QSIM Application will generate and execute SAS code that calculates summary statistics on the length of a queue. When you want to start collecting the sample data, you select the On radio button in the Simulation control panel. This starts data
collection. When you are ready to generate sample statistics select the component for which you want the statistics and then click the **Analyze** button. For example, you display data on the queue length on the single-queue multiple-server model in Figure 8.1 by selecting FIFOQueue 1 in the Simulation Control panel and then by pressing **Analyze**.

![Image](image.png)

**Figure 8.4.** Statistics on Queue Length

This generates the report shown in Figure 8.4 in the SAS Output Window. Figure 8.4 shows that the sample mean queue length is approximately 45.90 and that the sample variance is approximately 2.04.

The **Analyze** button also opens a graphics window with the histogram on the queue length as shown in Figure 8.5. This shows the sample distribution of queue length for the complete sample path that was collected from the time the **Collect Data** check box is selected until the time the **Analyze** button is selected.
It is important to note that the observations in the sample path are not independent. There can be a significant amount of autocorrelation in the observations of queue length.

**Another way to get Queue Length Statistics**

Another way you can obtain statistics on queue length and server utilization is by using the chart components. You take the queue that you want to monitor and drag it into one of the chart components, the VHistogram for example. When you drop the queue, a control panel will open from which you can select the attribute of the com-
ponent that you want sampled and the distribution to control sampling. Figure 8.6 shows an example. Here the size is selected to be monitored, and the component is to be sampled with a deterministic inter-sample time of one time unit. This is the default sampling distribution. This is different than using the Simulation control panel because in that case all state changes are captured, when using a chart component the queue state is sampled.

![Sample Component State Control Panel](image)

**Figure 8.6. Sample Component State Control Panel**

This control panel is opened when the queue labeled “ID: 1” in Figure 2.17 is dropped on the histogram.

![Vertical Histogram of the FIFO Queue length](image)

**Figure 8.7. Vertical Histogram of the FIFO Queue length**

Figure 2.17 also shows the histogram control panel opened. Notice that the control panel shows the simple statistics: minimum, maximum, mean, and standard deviation. Also note that when a component is dropped on a chart, a bucket is automatically
associated with the chart component. The bucket is where the sample is collected. The controls for this implicit bucket can be viewed by clicking the **Bin Controls** button in the Histogram Controls window. It opens the control panel for the bucket as shown in Figure 2.15.

![Bucket Control Panel](image)

Figure 8.8. Bucket Control Panel

You can display more detailed statistics on queue length using SAS data sets. The “Data Collection” section in the Bucket control panel shows a data collection **Status** check box. If this is selected, then data on the component state changes are routed to the SAS data set named WORK.BCKT_1. If sample data have been collected for a time, then clicking the **Analyze** button will generate a univariate analysis performed by the UNIVARIATE procedure and a histogram.

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**Server Utilization**

The utilization of a server is another measure of system performance that is often of interest. Estimates on the probability that a server is busy is one statistic for measuring utilization. If after collecting data using the **Collect Data** check box on the Simulation Control panel, you select a server from the components list box and click the **Analyze** button, you get a printout similar to that shown in Figure 8.9.
Figure 8.9. Statistics on Server Utilization

The mean shown is approximately .77. This is an estimate of the probability that the server is busy.
The pie chart in Figure 8.10 shows the percent of time that the server is busy.

Another way to get Server Utilization Statistics

Another way to view server utilization statistics is with a chart component. One component that can be used is the VHistogram. Figure 8.12 shows a VHistogram and a Histrogram control panel. This histogram had an MServer dropped on it and is monitoring the number of busy servers.
DATA Step Program for Extracting Information

When you click the Analyze button in the Simulation control panel (see Figure 8.3), the QSIM Application executes SAS code to extract and summarize the sample path saved in the WORK.SAMPLE data set. You, too, can write a SAS program to extract and analyze these data. For example, suppose you want to subset the data on the time the queue is in each state. The following DATA step subsets WORK.SAMPLE with those observations that have state information on queue with ID 5:

```sas
data subset;
  set sample;
  if id=5;
  keep timenow number time;
  label number="Queue Length";
  time = ( timenow - lag(timenow) );
  number = lag(state);
run;
```

The resulting data set has three variables: TIMENOW for the time that the state changes; NUMBER for the number in the queue; and TIME for the length of time in that state. The following SAS code executes the UNIVARIATE procedure to produce summary statistics and the GCHART procedure to produce a histogram as shown in Figure 8.5.

```sas
proc univariate data=subset;
  weight time;
  var number;
run;

proc gchart;
  label = "Time in Queue";
  vbar number / subvar=time discrete;
run;
```

A similar SAS program subsets the data on server utilization and produces the output in Figure 8.10 and Figure 8.9.

```sas
data subset;
  set sample;
  if id=4;
  keep timenow number time;
  label number="Utilization";
  time = ( timenow - lag(timenow) );
  number = lag(state);
run;

proc univariate data=subset;
  weight time;
  var busy;
run;
```
Statistics on Transaction State

As a transaction goes through the simulation, it maintains a history of the time spent at various components. When a transaction arrives at a Bucket, it can save any of its attributes. The name of the data set is derived from the number of buckets in the model and is displayed in the Bucket control panel as shown in Figure 2.15.

Time in the System

By default, the Bucket component accumulates the age or system time of the transactions arriving to it. However, it can accumulate any attribute of the transaction including user-defined attributes. The Bucket control panel has a check box which when set, records the attribute values in the SAS data set. Figure 2.15 shows such a control panel. If a simulation has been executing and the Collect Data check box has been set, then you can click the Analyze button to submit SAS code that calculates statistics on the sample.

Univariate statistics are calculated and histograms are printed for the attribute named in the Bucket control panel.

Figure 8.12. A Histogram Showing Time in the Queue

The control panel for the VHistogram maintains statistics on the sample in the Bucket and displays them as shown in Figure 8.12.